

### COURSE PROFILE

| Course Name         | Code        | Semester | Term | Theory<br>+PS+Lab.<br>(hour/week) | Local Credits | ECTS |
|---------------------|-------------|----------|------|-----------------------------------|---------------|------|
| Functional Analysis | MATH<br>314 | Spring   | 6    | 3+0+0                             | 3             | 8    |

|                      |      |
|----------------------|------|
| <b>Prerequisites</b> | None |
|----------------------|------|

|                                 |  |
|---------------------------------|--|
| <b>Course Language</b>          | English  |
| <b>Course Type</b>              | Required   |
| <b>Course Lecturer</b>          |  |
| <b>Course Assistant</b>         |  |
| <b>Course Objectives</b>        | The aim of the course is to introduce students to the elements of introductory Functional Analysis, metric and normed spaces, completeness and Banach spaces, inner product and Hilbert spaces and to introduce bounded linear operators.  |
| <b>Course Learning Outcomes</b> | By the end of the course the students should be able to:<br><ol style="list-style-type: none"> <li>1. to recognize metric spaces and normed spaces, understand the difference between the structure of fundamental function spaces, and handle a variety of metric and norm properties</li> <li>2. to prove elementary theorems involving the concepts of function spaces</li> </ol> |
| <b>Course Content</b>           | Elementary concepts. Metric spaces. Normed spaces. Banach spaces. Inner product, Orthogonality. Continuous linear transformations. The space of bounded linear operators.  |

### COURSE CONTENT

| Week | Subjects                         | Related Preparation |
|------|----------------------------------|---------------------|
| 1    | Linear Algebra                   | Chapter 1           |
| 2    | Metric spaces                    | Chapter 1           |
| 3    | Lebesgue Integration             | Chapter 1           |
| 4    | Example of Normed Spaces         | Chapter 2           |
| 5    | Finite-dimensional Normed Spaces | Chapter 2           |

|           |  |           |
|-----------|--|-----------|
| <b>6</b>  | Banach Spaces                            | Chapter 2 |
| <b>7</b>  | Inner Products                           | Chapter 3 |
| <b>8</b>  | Orthogonality, Orthogonal Complements    | Chapter 3 |
| <b>9</b>  | Orthonormal Bases in Infinite Dimensions | Chapter 3 |
| <b>10</b> | Fourier Series                           | Chapter 3 |
| <b>11</b> | Continuous Linear Transformations        | Chapter 4 |
| <b>12</b> | The Norm of a Bounded Linear Operator    | Chapter 4 |
| <b>13</b> | The Space $B(X,Y)$                       | Chapter 4 |
| <b>14</b> | Inverses of Operators                    | Chapter 4 |

|                               |   |
|-------------------------------|---|
| <b>Course Textbooks</b>       | Bryan P. Rynne and Martin A. Youngson: Linear Functional Analysis, second edition, Springer.                          |
| <b>Recommended References</b> | I.J. Maddox, Elements of Functional Analysis, second edition, Cambridge.<br>Peter D. Lax, Functional Analysis, Wiley. |

| <b>Semester Requirements</b>                      | <b>Number</b> | <b>Percentage of Grade</b> |
|---|---------------|----------------------------|
| Attendance/Participation                          | 1             | 5                          |
| Laboratory  | -             | -                          |
| Application                                       | -             | -                          |
| <b>Special Course Internship (Work Placement)</b> | -             | -                          |
| Quizzes/Studio Critics                            | -             | -                          |
| Homework Assignments                              | 13            | -                          |
| Presentation                                      | -             | -                          |
| Project   | -             | -                          |
| Seminar/Workshop                                  | -             | -                          |
| Midterms/Oral Exams                               | 2             | 60                         |

|                  |    |     |
|------------------|----|-----|
| Final/Resit Exam | 1  | 35  |
| <b>Total</b>     | 17 | 100 |

|                                    |    |     |
|------------------------------------|----|-----|
| <b>PERCENTAGE OF SEMESTER WORK</b> | 16 | 65  |
| <b>PERCENTAGE OF FINAL WORK</b>    | 1  | 35  |
| <b>Total</b>                       | 17 | 100 |

|                 |                                     |   |
|-----------------|-------------------------------------|---|
| Course Category | Core Courses                        | X |
|                 | Major Area Courses                  |   |
|                 | Supportive Courses                  |   |
|                 | Media and Management Skills Courses |   |
|                 | Transferable Skill Courses          |   |

#### COURSE'S CONTRIBUTION TO PROGRAM

| # | Program Qualifications / Outcomes  | * Level of Contribution |   |   |   |   |
|---|--|-------------------------|---|---|---|---|
|   |  | 1                       | 2 | 3 | 4 | 5 |
| 1 | To have a grasp of basic mathematics, applied mathematics and theories and applications of statistics.   |                         |   |   | X |   |
| 2 | To be able to use theoretical and applied knowledge acquired in the advanced fields of mathematics and statistics,   |                         |   |   |   | X |
| 3 | To be able to define and analyze problems and to find solutions based on scientific methods,   |                         |   |   |   | X |
| 4 | To be able to apply mathematics and statistics in real life with interdisciplinary approach and to discover their potentials,  |                         |   |   |   | X |
| 5 | To be able to acquire necessary information and to make modeling in any field that mathematics is used and to improve herself/himself,   |                         |   |   |   | X |
| 6 | To be able to criticize and renew her/his own models and solutions,  |                         |   |   |   | X |
| 7 | To be able to tell theoretical and technical information easily to both experts in detail and nonexperts in basic and comprehensible way,  |                         |   |   | X |   |
| 8 | To be able to use international resources in English and in a second foreign language from the European Language Portfolio (at the level of B1) effectively and to keep knowledge up-to-date, to communicate comfortably with colleagues from Turkey and other countries, to |                         |   |   | X |   |

|           |  |  |   |  |   |   |
|-----------|--|--|---|--|---|---|
|           | follow periodic literature,  |  |   |  |   |   |
| <b>9</b>  | To be familiar with computer programs used in the fields of mathematics and statistics and to be able to use at least one of them effectively at the European Computer Driving Licence Advanced Level,                                 |  | X |  |   |   |
| <b>10</b> | To be able to behave in accordance with social, scientific and ethical values in each step of the projects involved and to be able to introduce and apply projects in terms of civic engagement,                                       |  |   |  | X |   |
| <b>11</b> | To be able to evaluate all processes effectively and to have enough awareness about quality management by being conscious and having intellectual background in the universal sense,   |  |   |  | X |   |
| <b>12</b> | By having a way of abstract thinking, to be able to connect concrete events and to transfer solutions, to be able to design experiments, collect data, and analyze results by scientific methods and to interfere,                     |  |   |  |   | X |
| <b>13</b> | To be able to continue lifelong learning by renewing the knowledge, the abilities and the competencies which have been developed during the program, and being conscious about lifelong learning,                                      |  |   |  | X |   |
| <b>14</b> | To be able to adapt and transfer the knowledge gained in the areas of mathematics and statistics to the level of secondary school,   |  |   |  | X |   |
| <b>15</b> | To be able to conduct a research either as an individual or as a team member, and to be effective in each related step of the project, to take role in the decision process, to plan and manage the project by using time effectively. |  |   |  | X |   |

\*1 Lowest, 2 Low, 3 Average, 4 High, 5 Highest

#### ECTS ALLOCATED BASED ON STUDENT WORKLOAD BY THE COURSE DESCRIPTION

| Activities  | Number | Duration (Hours) | Total Workload |
|---|--------|------------------|----------------|
| <b>Course Hours (Including Exams)</b>             | 14     | 3                | 48             |
| <b>Tutorials</b>                                  | -      | -                | -              |
| <b>Laboratory</b>                                 | -      | -                | -              |
| <b>Application</b>                                | -      | -                | -              |
| <b>Special Course Internship (Work Placement)</b> | -      | -                | -              |
| <b>Field Work</b>                                 | -      | -                | -              |
| <b>Study Hours Out of Class</b>                   | 14     | 4                | 56             |

|                                |    |                       |            |
|--------------------------------|----|-----------------------|------------|
| <b>Presentations / Seminar</b> | -  | -                     | -          |
| <b>Project</b>                 | -  | -                     | -          |
| <b>Preparatory reading</b>     | 13 | 2                     | 26         |
| <b>Homework Assignments</b>    | 13 | 4                     | 52         |
| <b>Quizzes</b>                 | -  | -                     | -          |
| <b>Midterm Exams</b>           | 2  | 4                     | 8          |
| <b>Final / Resit Exam</b>      | 1  | 10                    | 10         |
|                                |    | <b>Total Workload</b> | <b>200</b> |

#### COURSE CATEGORY

| <b>ISCED<br/>GENERAL<br/>AREA<br/>CODES</b> | <b>GENERAL AREAS</b>                 | <b>ISCED<br/>BASIC AREA<br/>CODES</b> | <b>BASIC EDUCATIONAL AREAS</b>            |     |
|---|--------------------------------------|---------------------------------------|---|-----|
| 1   | Education                            | 14                                    | Teacher Training and Educational Sciences | 0   |
| 2   | Humanities and Art                   | 21                                    | Art                                       | 0   |
| 2   | Humanities and Art                   | 22                                    | Humanities                                | 0   |
| 3   | Social Sciences, Management and Law  | 31                                    | Social and Behavioral Sciences            | 0   |
| 3   | Social Sciences, Management and Law  | 32                                    | Journalism and Informatics                | 0   |
| 3   | Social Sciences, Management and Law  | 38                                    | Law                                       | 0   |
| 4   | Science                              | 42                                    | Life Sciences                             | 0   |
| 4   | Science                              | 44                                    | Natural Sciences                          | 0   |
| 4   | Science                              | 46                                    | Mathematics and Statistics                | 100 |
| 4   | Science                              | 48                                    | Computer                                  | 0   |
| 5   | Engineering, Manufacturing and Civil | 52                                    | Engineering                               | 0   |
| 5   | Engineering, Manufacturing and Civil | 54                                    | Manufacturing and Processing              | 0   |
| 5   | Engineering, Manufacturing and Civil | 58                                    | Architecture and Structure                | 0   |

|   |                      |    |   |   |
|---|----------------------|----|---|---|
| 6 | Agriculture          | 62 | Agriculture, Forestry, Livestock, Fishery | 0 |
| 6 | Agriculture          | 64 | Veterinary                                | 0 |
| 7 | Medicine and Welfare | 72 | Medical                                   | 0 |
| 7 | Medicine and Welfare | 76 | Social Services                           | 0 |
| 8 | Service              | 81 | Personal Services                         | 0 |
| 8 | Service              | 84 | Transport Services                        | 0 |
| 8 | Service              | 85 | Environment Protection                    | 0 |
| 8 | Service              | 86 | Security Services                         | 0 |